

**AML-CS**

APPLIED MATH AND COMPUTER SCIENCE LAB

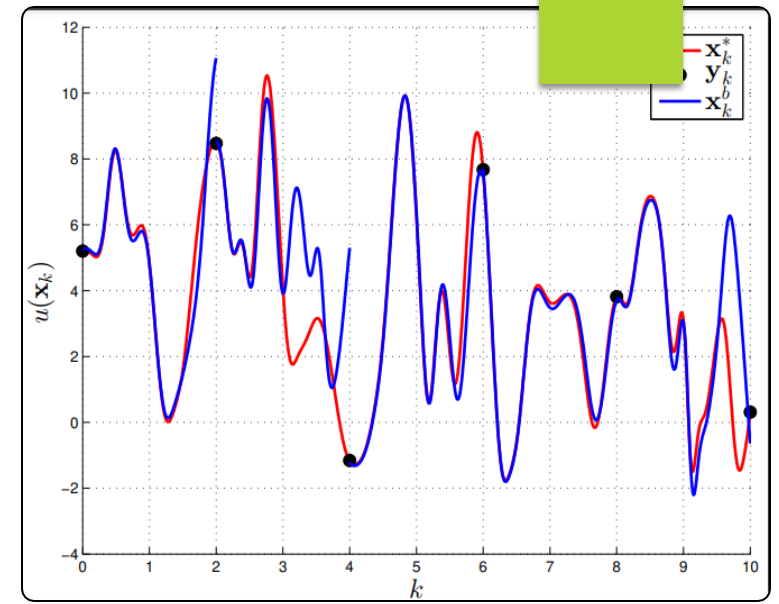
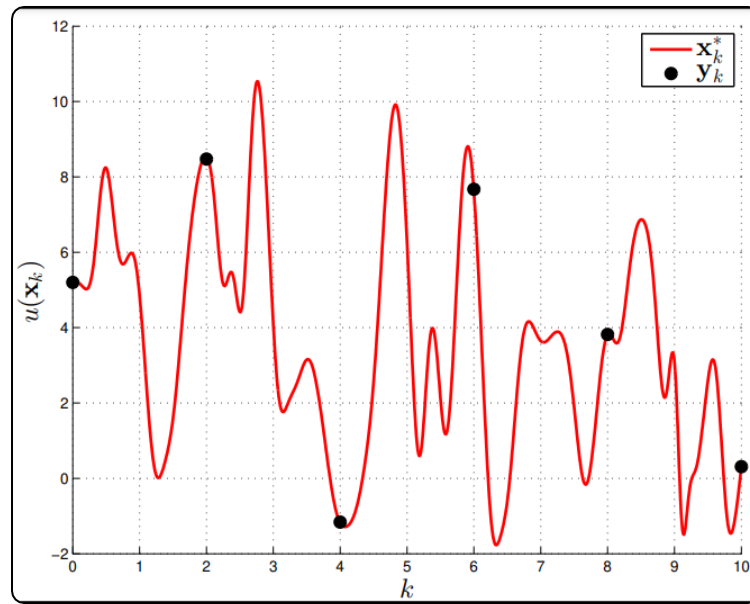
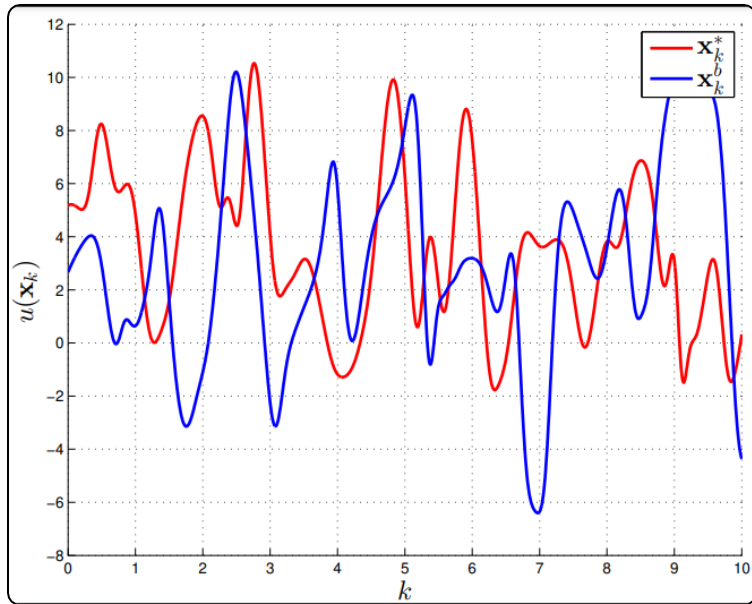


# Data Assimilation

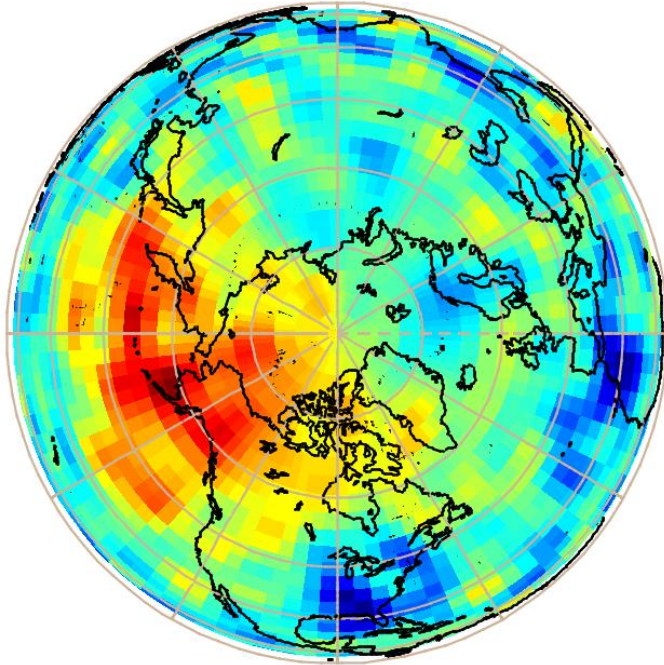
ELÍAS D. NIÑO RUIZ

# What is Data Assimilation?

- ▶ Data Assimilation is the process by which an imperfect numerical forecast is adjusted according to real-noisy observations.



# Data Assimilation Process (Sequential)



Are  
forecasts  
enough?

# Forecasts

Numerical Models =  
Prior Knowledge

Initial Value  
Problem

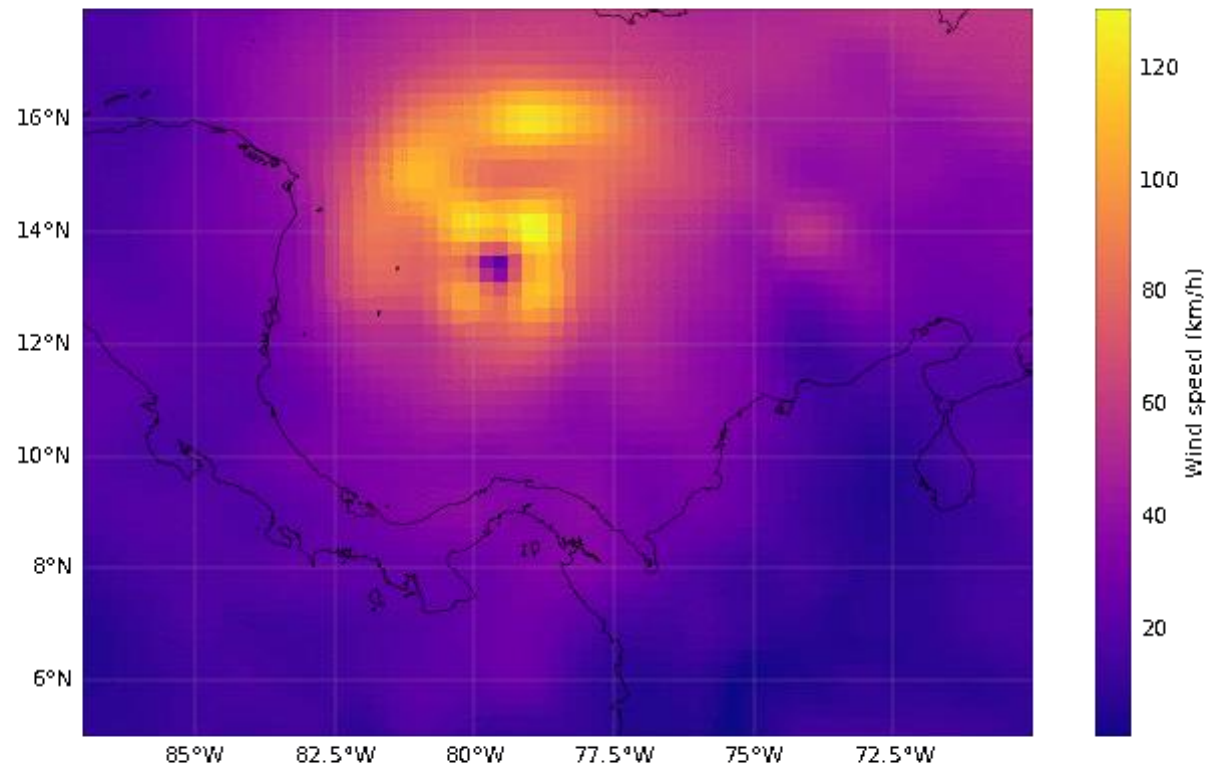
Errors  
on Initial Conditions

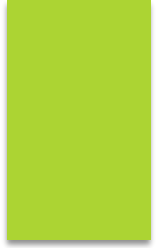
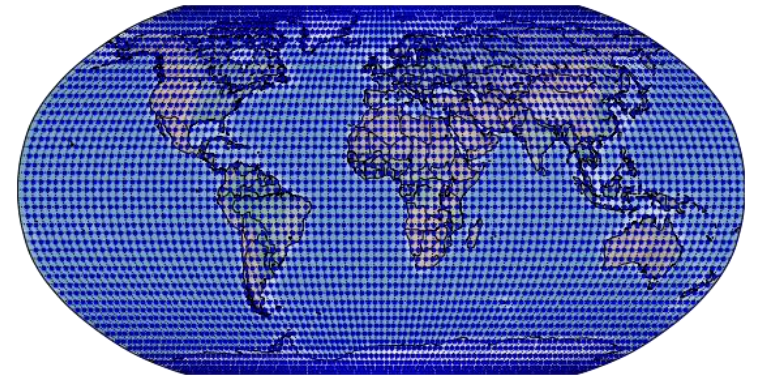
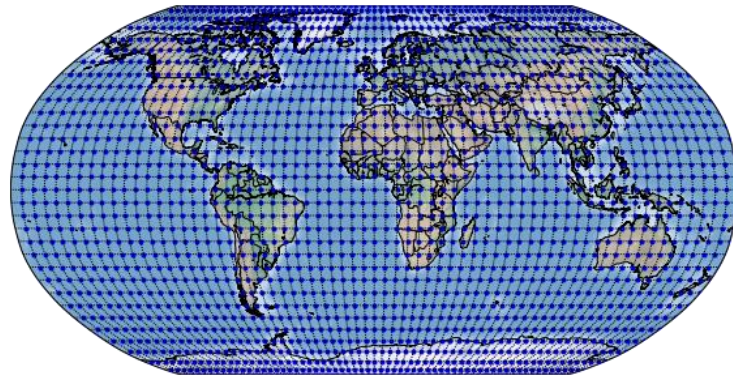
Discretization –  
Spatial Coverage

Discretization Errors

Numerical  
Integration

# Iota Hurricane – Nov 16, 2022





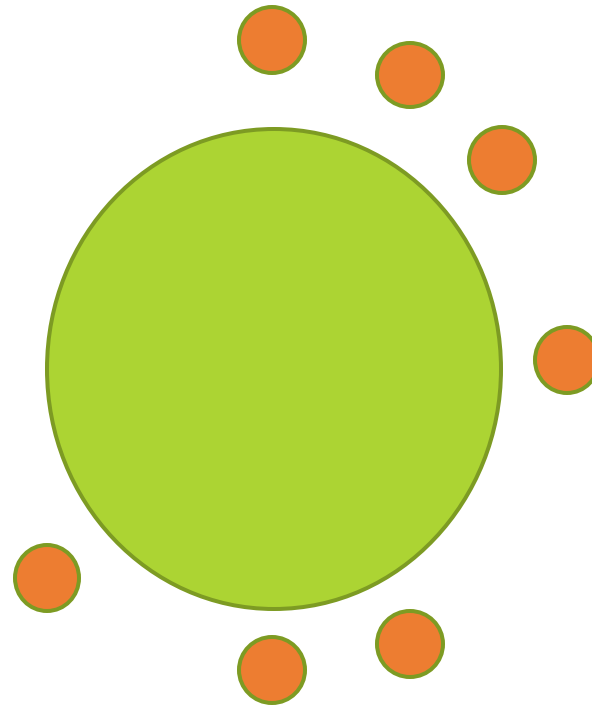
# Discretization

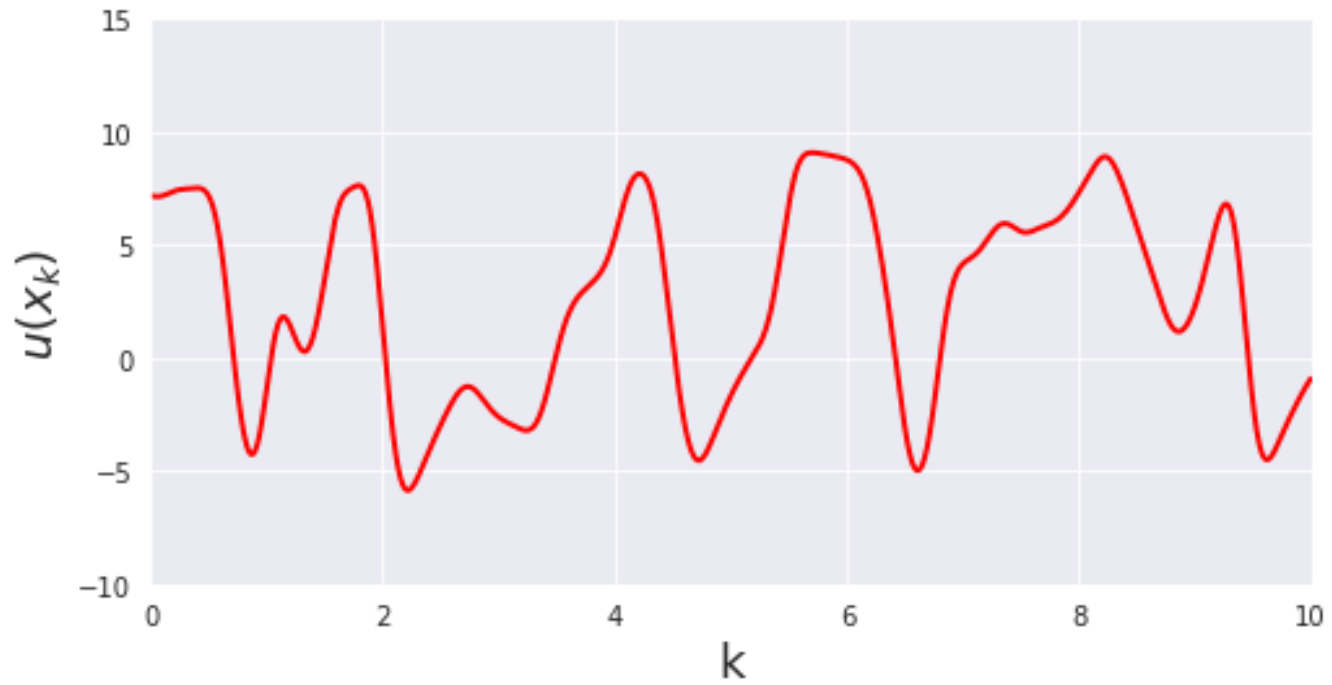
Nature  
is Chaotic



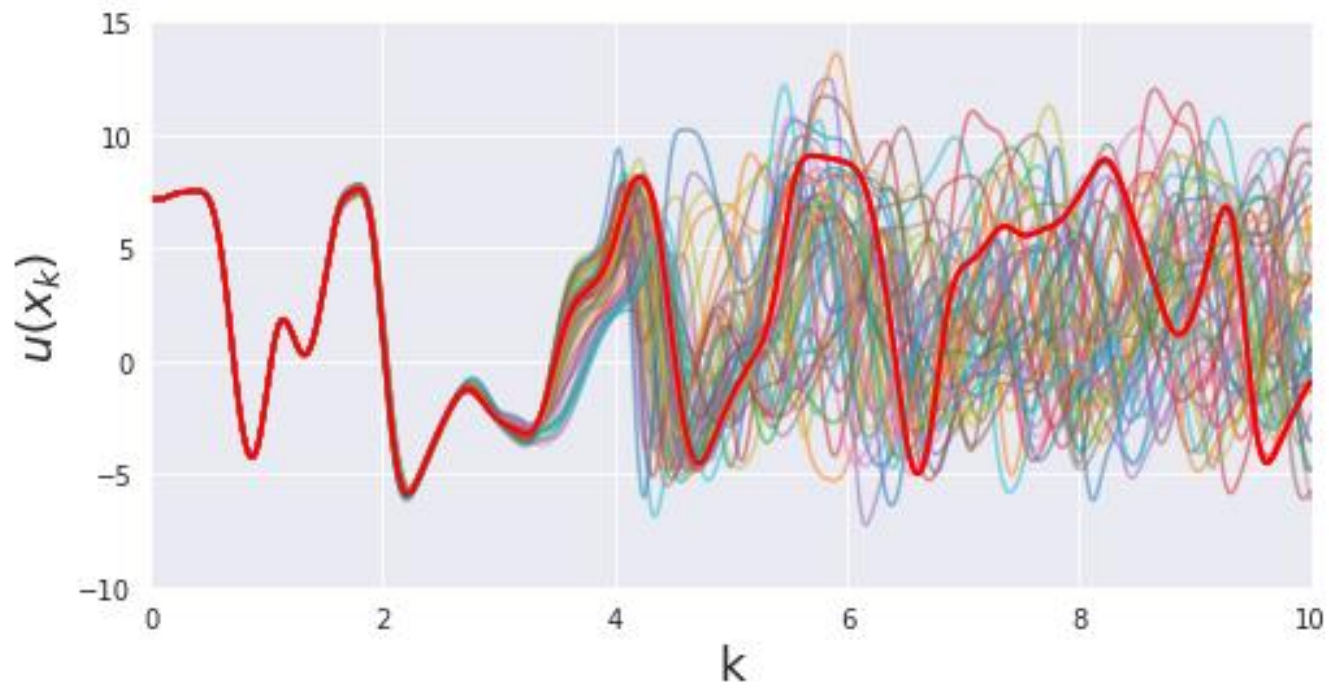
# Lorenz 96 Model

$$\frac{dx_i}{dt} = (x_{i+1} - x_{i-2})x_{i-1} - x_i + F$$

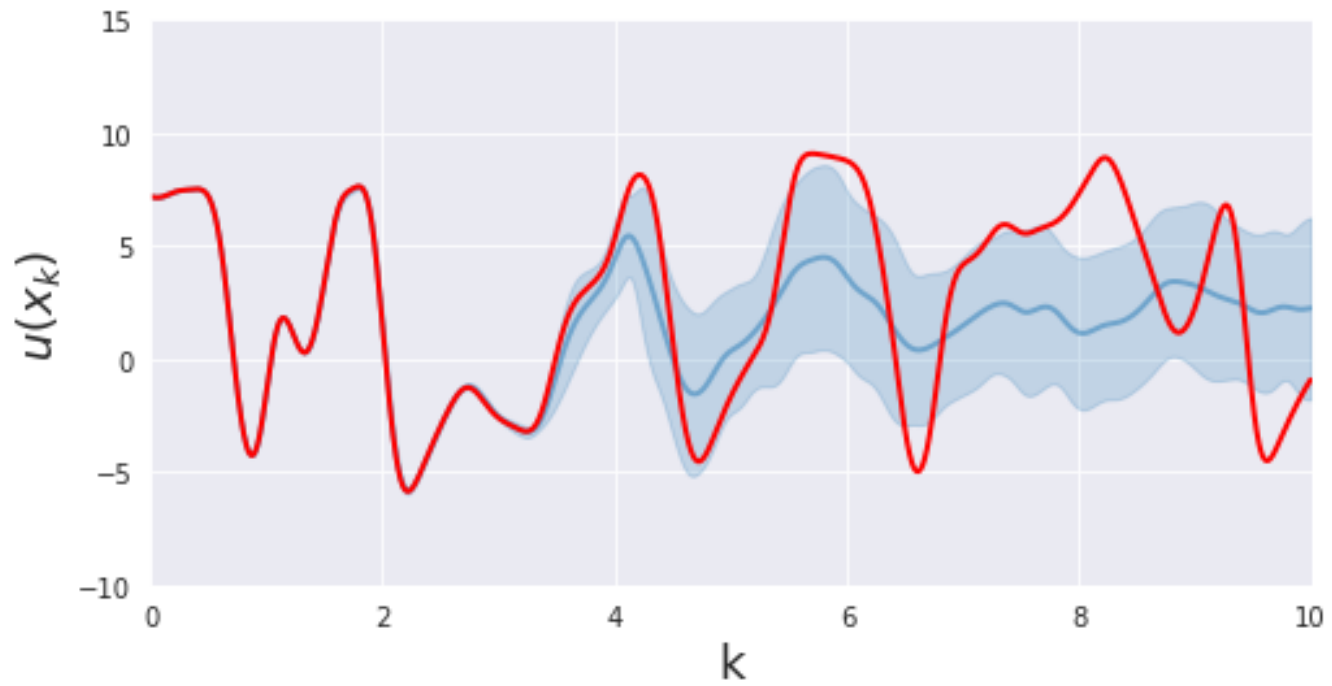




Lorenz  
96



Lorenz  
96



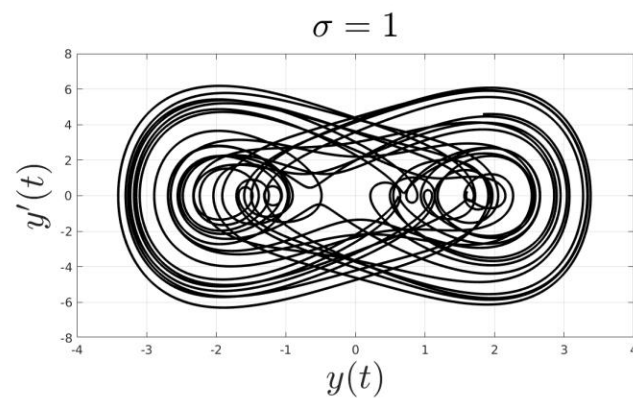
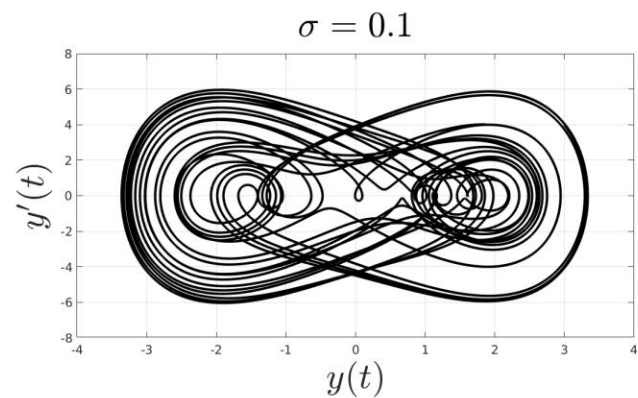
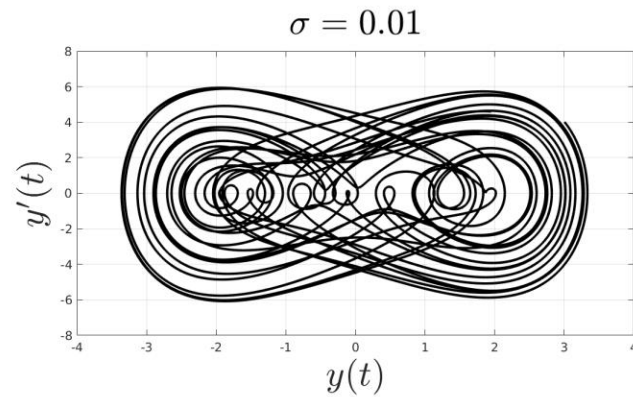
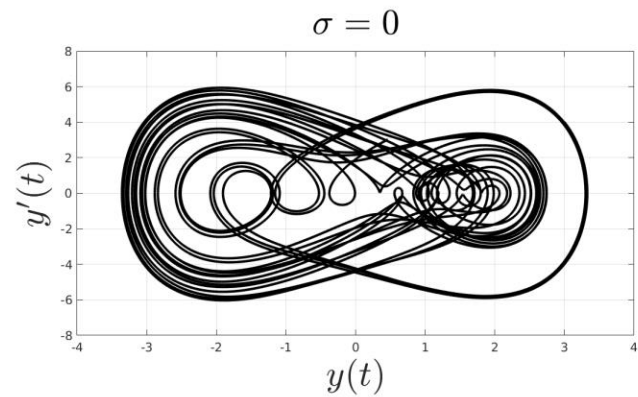
Lorenz  
96

# Duffing's Equation

- ▶ Non-linear second order differential equation
- ▶ Damped and Driven oscillators

$$x'' + \delta x' + \alpha x + \beta x^3 = \gamma \cos(\omega t)$$

# Duffing's Equation



# Forecasts

Uncertainty

Small errors are amplified

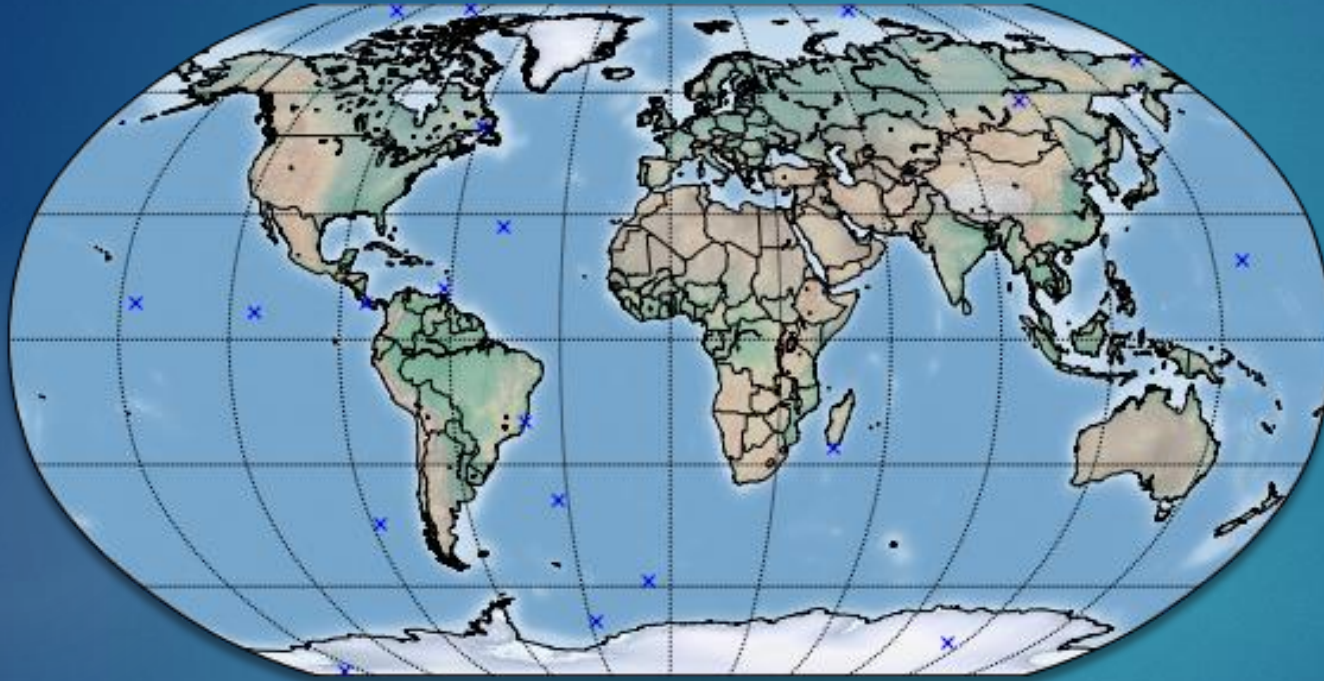
Initial condition

Computational cost

Physics simplifications

Understanding

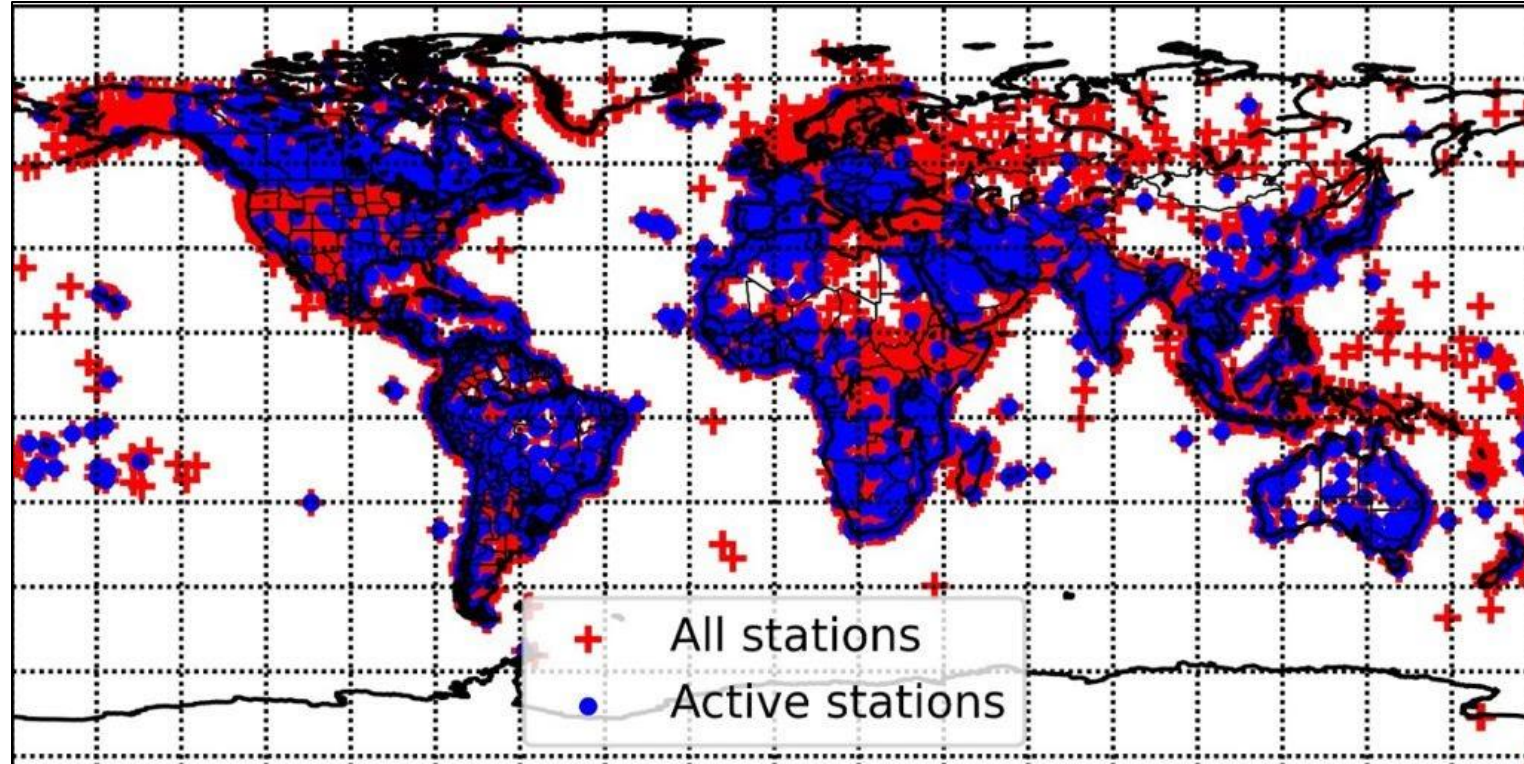
Discretization

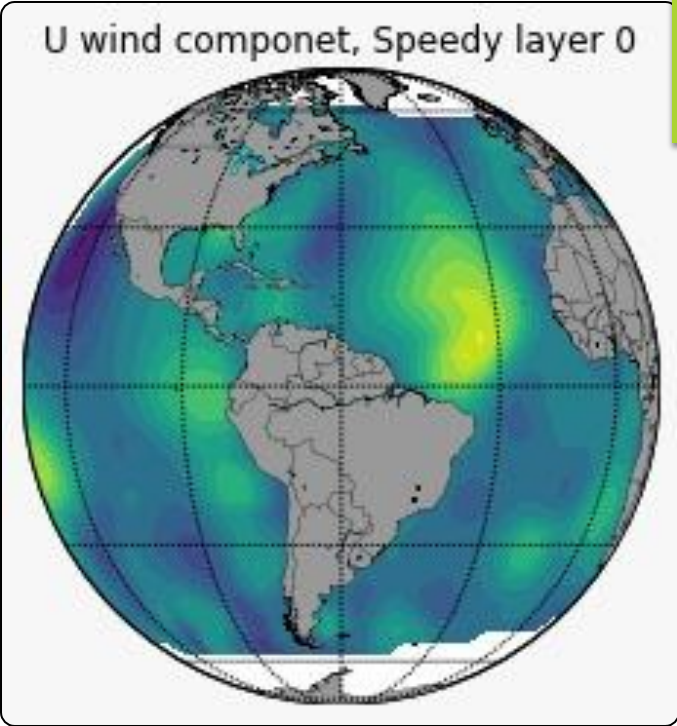
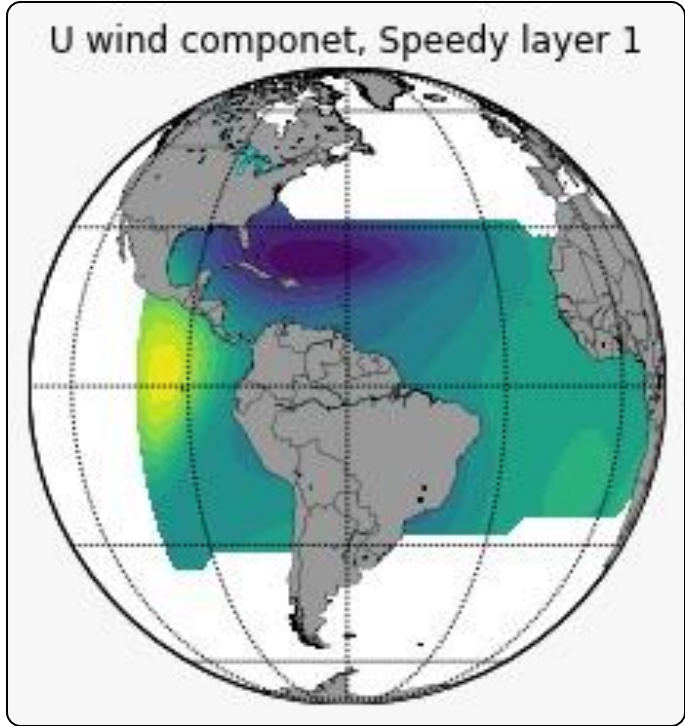


Are  
observations  
enough?



# OGIMET Network





# Machine Learning – Spatial Coverage

# Observations



Sparse observational networks



Error estimation

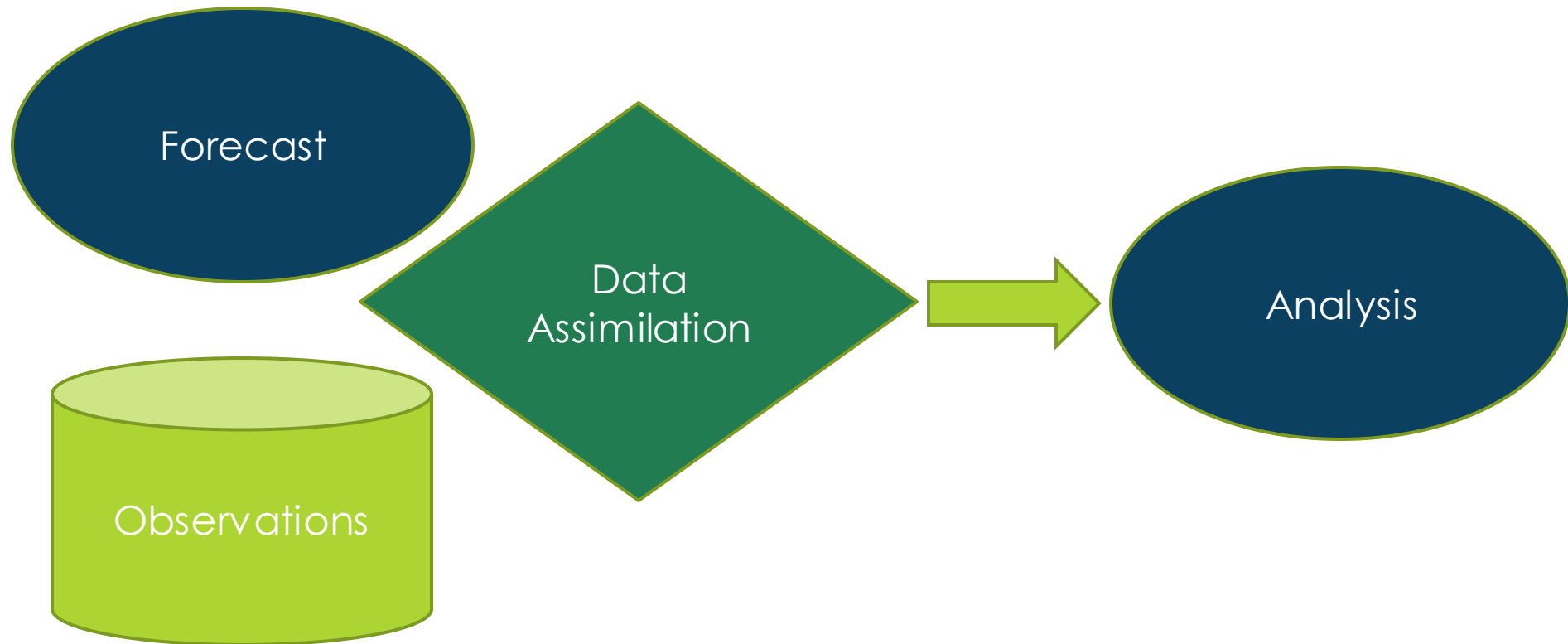


Extrapolation (forecasting)



Can we  
combine  
both  
sources of  
information?

# Sequential Data Assimilation



# Errors



Background



Observation



Analysis

# Topics

Background